

Fourth Semester B.E. Degree Examination, Dec. 2013/Jan. 2014
Field Theory

Time: 3 hrs.

Max. Marks: 100

**Note: Answer FIVE full questions, selecting
atleast TWO questions from each part.**

PART - A

1.
 - a. State and explain Gauss's law. (06 Marks)
 - b. Find electric field intensity E at $(0, 0, 5)m$ due to charge Q_1 at $(0, 4, 0)m$ and charge Q_2 at $(3, 0, 0)m$. The charges are $Q_1 = 0.35$ micro coulombs and $Q_2 = -0.55$ micro coulombs respectively. Hence find magnitude and direction of E . (08 Marks)
 - c. Find the total charge in a volume defined by six planes for which $1 \leq x \leq 2$; $2 \leq y \leq 3$; and $3 \leq z \leq 4$ if $D = (4x\hat{a}_x + 3y^2\hat{a}_y + 2z^3\hat{a}_z) \text{ c/m}^2$. (06 Marks)

2.
 - a. Find the work done in moving a charge $Q = 20$ micro-coulombs in the electric field given by

$$E = \left(\frac{x}{2} + 2y\right)\hat{a}_x + 2x\hat{a}_y \text{ v/m}$$
 - i) $(0, 0, 0)m$ to $(4, 0, 0)m$
 - ii) $(4, 0, 0)m$ to $(4, 2, 0)m$. (06 Marks)
 - b. Obtain the boundary conditions between conductor and free space. (08 Marks)
 - c. Derive an expression for capacitance of two concentric spherical shells. (06 Marks)

3.
 - a. Explain Poisson's and Laplace's equation. (06 Marks)
 - b. State and prove uniqueness theorem. (08 Marks)
 - c. Let $V = \frac{\cos 2\phi}{\rho}$ in free space. Find the volume charge density at point $A(\rho = 0.5, \phi = 60^\circ, z = 1)$. (06 Marks)

4.
 - a. Show that $\text{curl } H = J$ in a steady magnetic field. (08 Marks)
 - b. Find the magnetic field intensity and flux density at a point P for the current circuit shown in Fig. Q4(b). (08 Marks)

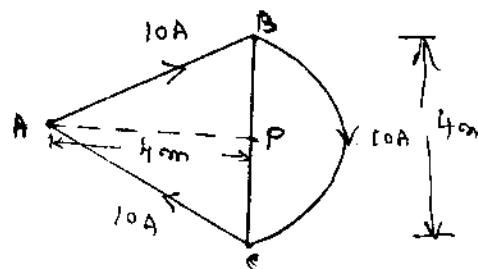


Fig. Q4(b)

- c. State and explain Stoke's theorem. (04 Marks)

PART – B

- 5 a. Find an expression for the force on a differential current carrying element. (08 Marks)
 b. Obtain the relationship between α_1 and α_2 in terms of relative permeabilities of the two media μ_{r1} and μ_{r2} . (06 Marks)
 Derive an expression for the inductance of a co-axial cable. (08 Marks)
- 6 a. State Faraday's law and obtain point and integral form of electromagnetic induction. (06 Marks)
 b. If the electric field intensity in free space is given by $E = E_m \sin(\alpha x) \sin(\omega t - \beta z) \hat{a}_y$ v/m, find the magnetic field intensity using Faraday's law. (08 Marks)
 c. Write Maxwell's equation in point form and in integral form for time varying fields. (06 Marks)
- 7 a. Starting from Maxwell's equation, derive the wave equation for a uniform plane wave traveling in free space. (10 Marks)
 b. State and prove Poynting's theorem and show that $P = E \times H$. (10 Marks)
- 8 a. Show that at any instant "t", the magnetic and electric field in a reflected wave are out of phase by 90° . (10 Marks)
 b. With necessary expression, explain standing wave ratio (SWR). (10 Marks)
